

STAT810 Statistical Theory

S1 External 2014

Statistics

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General Information

Unit convenor and teaching staff Other Staff Thomas Fung thomas.fung@mq.edu.au

Contact via thomas.fung@mq.edu.au E4A 530 Monday 2 - 4 pm

Unit Convenor Ian Marschner ian.marschner@mq.edu.au Contact via ian.marschner@mq.edu.au E4A 540 11am Wednesday

Credit points

4

Prerequisites

Admission to MAppStat or PGDipAppStat or PGCertAppStat or (ACST601 and ACST602 and ACST604)

Corequisites

Co-badged status

Unit description

This unit introduces the fundamental principles of statistical inference and estimation theory. The unit begins with a discussion of probability concepts, including relative frequency, random variables, distributions and large sample theory. A discussion of estimation concepts is provided, particularly unbiasedness, consistency and efficiency. Likelihood theory is then developed, including the concept of sufficiency and the maximum likelihood approach to estimation. Hypothesis testing concepts and methods are discussed with a particular focus on likelihood ratio, score and Wald tests. An introduction to Bayesian inference principles is also provided.

Important Academic Dates

Information about important academic dates including deadlines for withdrawing from units are available at https://www.mq.edu.au/study/calendar-of-dates

Learning Outcomes

On successful completion of this unit, you will be able to:

be familiar with techniques to calculate probabilities, expected values and probability, moment and cumulant generating functions for discrete, continuous and multivariate random variables and know how to apply these concepts in practical problems understand fundamental limit theorems of Probability and Statistics and be able to apply them in practical problems understand three modes of convergence of random variables and be able to apply them to get practical large sample approximations understand and know how to use the Delta Method in practical problems understand the principles and theory of estimation understand the principles and theory of statistical hypothesis testing

Assessment Tasks

Name	Weighting	Due
Assignment 1	15%	25 March 2014
Assignment 2	15%	29 April 2014
Assignment 3	15%	20 May 2014
Mid-year examination	55%	To be determined

Assignment 1

Due: 25 March 2014

Weighting: 15%

Assignment 1

On successful completion you will be able to:

- be familiar with techniques to calculate probabilities, expected values and probability, moment and cumulant generating functions for discrete, continuous and multivariate random variables and know how to apply these concepts in practical problems
- understand fundamental limit theorems of Probability and Statistics and be able to apply them in practical problems

Assignment 2

Due: 29 April 2014 Weighting: 15%

Assignment 2

On successful completion you will be able to:

- understand three modes of convergence of random variables and be able to apply them to get practical large sample approximations
- understand and know how to use the Delta Method in practical problems

Assignment 3

Due: 20 May 2014 Weighting: 15%

Assignment 3

On successful completion you will be able to:

- understand the principles and theory of estimation
- · understand the principles and theory of statistical hypothesis testing

Mid-year examination

Due: **To be determined** Weighting: **55%**

Mid-year examination

On successful completion you will be able to:

- be familiar with techniques to calculate probabilities, expected values and probability, moment and cumulant generating functions for discrete, continuous and multivariate random variables and know how to apply these concepts in practical problems
- understand fundamental limit theorems of Probability and Statistics and be able to apply them in practical problems
- understand three modes of convergence of random variables and be able to apply them to get practical large sample approximations
- · understand and know how to use the Delta Method in practical problems
- · understand the principles and theory of estimation
- understand the principles and theory of statistical hypothesis testing

Delivery and Resources

LECTURE NOTES AND OTHER MATERIALS

Lecture notes and audio recordings of lectures will be made available to external students via the unit's iLearn website (see Internet Resources below).

SOFTWARE

The R software package will be used for simulation and graphics. This software is freely available to be downloaded at www.r-project.org

TEXTBOOK

Mathematical Statistics with Applications, Seventh Edition. D.D. Wackerly, W. Mendenhall, R.L. Scheaffer. Duxbury Press.

This textbook will provide additional readings and problems, to supplement the lecture and tutorial material.

INTERNET RESOURCES / TECHNOLOGIES USED

This unit has an iLearn website available at https://ilearn.mq.edu.au/login/MQ/

Lecture notes: these will be available on the iLearn site prior to the lecture.

Audio recordings: all lectures will be recorded and will be available after the lecture.

Consult the iLearn website frequently. Other resources available include a discussion board, assignments, administrative updates etc.

CONSULTATION

Lecturers are available for consultation through iLearn and email, as well as during published consultation hours. For all administrative communications external students should contact:

Lesley Mooney

(02) 9850-8550

lesley.mooney@mq.edu.au

Building E4A room 550

ASSIGNMENT SUBMISSION

Students may submit assignments during the lecture or via the iLearn website.

CHANGES SINCE LAST DELIVERY

No substantive changes since last delivery

Unit Schedule

Week 1: Introduction to Probability and Statistics. Discrete random variables and their probability distributions.

Week 2: Continuous random variables and their probability distributions. Probability, Moment and Cumulant Generating Functions.

Week 3: Multivariate probability distributions. Functions of random variables.

Weeks 4 – 7: Laws of Large Numbers, Central Limit Theorem, Asymptotic Theory.

Weeks 8 – 10: Estimation, properties of estimators, likelihood theory.

Week 11 – 13: Hypotheses testing, properties of tests, likelihood-based inference methods, Bayesian inference.

Policies and Procedures

Macquarie University policies and procedures are accessible from Policy Central. Students should be aware of the following policies in particular with regard to Learning and Teaching:

Academic Honesty Policy <u>http://mq.edu.au/policy/docs/academic_honesty/policy.ht</u> ml

Assessment Policy http://mq.edu.au/policy/docs/assessment/policy.html

Grading Policy http://mq.edu.au/policy/docs/grading/policy.html

Grade Appeal Policy http://mq.edu.au/policy/docs/gradeappeal/policy.html

Grievance Management Policy <u>http://mq.edu.au/policy/docs/grievance_managemen</u> t/policy.html

Disruption to Studies Policy <u>http://www.mq.edu.au/policy/docs/disruption_studies/policy.html</u> The Disruption to Studies Policy is effective from March 3 2014 and replaces the Special Consideration Policy.

In addition, a number of other policies can be found in the <u>Learning and Teaching Category</u> of Policy Central.

Student Code of Conduct

Macquarie University students have a responsibility to be familiar with the Student Code of Conduct: https://students.mq.edu.au/support/student_conduct/

Policy on Late submission of Assignments

No extensions will be granted. Students who have not submitted an assignment prior to the deadline will be awarded a mark of 0 for the task, except for cases in which an application for special consideration is made and approved.

Student Support

Macquarie University provides a range of support services for students. For details, visit <u>http://stu</u> dents.mq.edu.au/support/

Learning Skills

Learning Skills (<u>mq.edu.au/learningskills</u>) provides academic writing resources and study strategies to improve your marks and take control of your study.

- Workshops
- StudyWise
- Academic Integrity Module for Students
- Ask a Learning Adviser

Student Services and Support

Students with a disability are encouraged to contact the **Disability Service** who can provide appropriate help with any issues that arise during their studies.

Student Enquiries

For all student enquiries, visit Student Connect at ask.mq.edu.au

IT Help

For help with University computer systems and technology, visit <u>http://informatics.mq.edu.au/hel</u>p/.

When using the University's IT, you must adhere to the <u>Acceptable Use Policy</u>. The policy applies to all who connect to the MQ network including students.

Graduate Capabilities

PG - Discipline Knowledge and Skills

Our postgraduates will be able to demonstrate a significantly enhanced depth and breadth of knowledge, scholarly understanding, and specific subject content knowledge in their chosen

fields.

This graduate capability is supported by:

Learning outcomes

- be familiar with techniques to calculate probabilities, expected values and probability, moment and cumulant generating functions for discrete, continuous and multivariate random variables and know how to apply these concepts in practical problems
- understand fundamental limit theorems of Probability and Statistics and be able to apply them in practical problems
- understand three modes of convergence of random variables and be able to apply them to get practical large sample approximations
- · understand and know how to use the Delta Method in practical problems
- · understand the principles and theory of estimation
- understand the principles and theory of statistical hypothesis testing

Assessment tasks

- Assignment 1
- Assignment 2
- Assignment 3
- Mid-year examination

PG - Critical, Analytical and Integrative Thinking

Our postgraduates will be capable of utilising and reflecting on prior knowledge and experience, of applying higher level critical thinking skills, and of integrating and synthesising learning and knowledge from a range of sources and environments. A characteristic of this form of thinking is the generation of new, professionally oriented knowledge through personal or group-based critique of practice and theory.

This graduate capability is supported by:

Learning outcomes

- · understand the principles and theory of estimation
- · understand the principles and theory of statistical hypothesis testing

Assessment tasks

- Assignment 3
- Mid-year examination

PG - Research and Problem Solving Capability

Our postgraduates will be capable of systematic enquiry; able to use research skills to create

new knowledge that can be applied to real world issues, or contribute to a field of study or practice to enhance society. They will be capable of creative questioning, problem finding and problem solving.

This graduate capability is supported by:

Learning outcomes

- be familiar with techniques to calculate probabilities, expected values and probability, moment and cumulant generating functions for discrete, continuous and multivariate random variables and know how to apply these concepts in practical problems
- understand fundamental limit theorems of Probability and Statistics and be able to apply them in practical problems
- understand three modes of convergence of random variables and be able to apply them to get practical large sample approximations
- · understand and know how to use the Delta Method in practical problems

Assessment tasks

- Assignment 1
- Assignment 2
- Mid-year examination

PG - Effective Communication

Our postgraduates will be able to communicate effectively and convey their views to different social, cultural, and professional audiences. They will be able to use a variety of technologically supported media to communicate with empathy using a range of written, spoken or visual formats.

This graduate capability is supported by:

Learning outcomes

- understand the principles and theory of estimation
- · understand the principles and theory of statistical hypothesis testing

Assessment tasks

- Assignment 3
- Mid-year examination

PG - Capable of Professional and Personal Judgment and Initiative

Our postgraduates will demonstrate a high standard of discernment and common sense in their professional and personal judgment. They will have the ability to make informed choices and decisions that reflect both the nature of their professional work and their personal perspectives.

This graduate capability is supported by:

Learning outcomes

- understand the principles and theory of estimation
- · understand the principles and theory of statistical hypothesis testing

Assessment tasks

- Assignment 3
- Mid-year examination

Changes since First Published

Date	Description
16/01/2014	The Prerequisites was updated.