

# MATH701

# Analysis

S1 Day 2015

Dept of Mathematics

# Contents

General Information	2
Learning Outcomes	2
General Assessment Information	3
Assessment Tasks	3
Delivery and Resources	6
Unit Schedule	6
Learning and Teaching Activities	7
Policies and Procedures	7
Graduate Capabilities	8

#### Disclaimer

Macquarie University has taken all reasonable measures to ensure the information in this publication is accurate and up-to-date. However, the information may change or become out-dated as a result of change in University policies, procedures or rules. The University reserves the right to make changes to any information in this publication without notice. Users of this publication are advised to check the website version of this publication [or the relevant faculty or department] before acting on any information in this publication.

# **General Information**

Unit convenor and teaching staff Lecturer Xuan Duong xuan.duong@mq.edu.au Contact via E-mail E7A207

Credit points 4

Prerequisites Admission to MRes

Corequisites

Co-badged status

#### Unit description

This unit provides an advanced introduction to the key areas of research interest in modern analysis. We will study Lebesgue integration, positive Borel measures, and the all important function spaces Lp. Then we will study the elementary Hilbert space theory and Banach space techniques. This will provide familiarity with some of the major theorems which make up the analysis toolbox: Monotone and Dominated Convergence theorems; Fatou's lemma; Egorov's theorem; Lusin's theorem; Radon-Nikodym theorem; Fubini-Tonelli theorems about product measures and integration on product spaces; Uniform Boundedness; Fundamental Theorem of Calculus for Lebesgue Integrals; Minkowski's Inequality; Holder's Inequality; Jensen's Inequality; and Bessel's Inequality.

#### Important Academic Dates

Information about important academic dates including deadlines for withdrawing from units are available at <a href="https://www.mq.edu.au/study/calendar-of-dates">https://www.mq.edu.au/study/calendar-of-dates</a>

# **Learning Outcomes**

On successful completion of this unit, you will be able to:

1. Understanding logical arguments and recognising any gaps or faults in such arguments.

2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.

3. Expressing yourself clearly and logically in writing

4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

# **General Assessment Information**

Each assignment has 5 or 6 questions taken from the textbook Real and Complex Analysis of Walter Rudin.

# Assessment Tasks

Name	Weighting	Due
Assignment 1	20%	Week 4
Assignment 2	20%	Week 7
Assignment 3	20%	Week 9
Assignment 4	20%	Week 11
Assignment 5	20%	Week 13

# Assignment 1

#### Due: Week 4 Weighting: 20%

This Assessment Task relates to the following Learning Outcomes:

- Understanding logical arguments and recognising any gaps or faults in such arguments.
- Solving problems, including: formulating a precise mathematical question from a "real world"

problem; identifying and applying appropriate mathematical techniques.

· Expressing yourself clearly and logically in writing

• More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

On successful completion you will be able to:

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real

world" problem; identifying and applying appropriate mathematical techniques.

- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assignment 2

Due: Week 7 Weighting: 20%

This Assessment Task relates to the following Learning Outcomes:

- Understanding logical arguments and recognising any gaps or faults in such arguments.
- Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- · Expressing yourself clearly and logically in writing
- More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

On successful completion you will be able to:

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

# Assignment 3

#### Due: Week 9 Weighting: 20%

This Assessment Task relates to the following Learning Outcomes:

- Understanding logical arguments and recognising any gaps or faults in such arguments.
- Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.

· Expressing yourself clearly and logically in writing

• More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

On successful completion you will be able to:

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

# Assignment 4

Due: Week 11 Weighting: 20%

This Assessment Task relates to the following Learning Outcomes:

• Understanding logical arguments and recognising any gaps or faults in such arguments.

• Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.

· Expressing yourself clearly and logically in writing

• More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

On successful completion you will be able to:

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical

analysis, problem solving and creative thinking.

#### Assignment 5

Due: Week 13 Weighting: 20%

This Assessment Task relates to the following Learning Outcomes:

• Understanding logical arguments and recognising any gaps or faults in such arguments.

• Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.

· Expressing yourself clearly and logically in writing

 More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

On successful completion you will be able to:

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- · 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### **Delivery and Resources**

Main textbook is W. Rudin's "Real and complex analysis"

# **Unit Schedule**

The first five chapters of W. Rudin's book "Real and complex analysis":

- Chapter 1: Abstract Integration
- Chapter 2: Positive Borel measures
- Chapter 3: Lp spaces
- Chapter 4: Elementary Hilbert space theory
- Chapter 5: Examples of Banach space techniques

Each of Chapters 1, 2, 4 and 5 takes an average of 5 hours lecturing, and Chapter 3 takes 4 hours.

The last week is for any unforseen delay.

# **Learning and Teaching Activities**

#### Lectures

Lectures

# **Policies and Procedures**

Macquarie University policies and procedures are accessible from <u>Policy Central</u>. Students should be aware of the following policies in particular with regard to Learning and Teaching:

Academic Honesty Policy http://mq.edu.au/policy/docs/academic\_honesty/policy.html

Assessment Policy http://mq.edu.au/policy/docs/assessment/policy.html

Grading Policy http://mq.edu.au/policy/docs/grading/policy.html

Grade Appeal Policy http://mq.edu.au/policy/docs/gradeappeal/policy.html

Grievance Management Policy http://mq.edu.au/policy/docs/grievance\_management/policy.html

Disruption to Studies Policy <u>http://www.mq.edu.au/policy/docs/disruption\_studies/policy.html</u> The Disruption to Studies Policy is effective from March 3 2014 and replaces the Special Consideration Policy.

In addition, a number of other policies can be found in the Learning and Teaching Category of Policy Central.

#### **Student Code of Conduct**

Macquarie University students have a responsibility to be familiar with the Student Code of Conduct: https://students.mq.edu.au/support/student\_conduct/

#### Results

Results shown in *iLearn*, or released directly by your Unit Convenor, are not confirmed as they are subject to final approval by the University. Once approved, final results will be sent to your student email address and will be made available in <u>eStudent</u>. For more information visit <u>ask.m</u> <u>q.edu.au</u>.

# Student Support

Macquarie University provides a range of support services for students. For details, visit <u>http://stu</u> dents.mq.edu.au/support/

#### **Learning Skills**

Learning Skills (<u>mq.edu.au/learningskills</u>) provides academic writing resources and study strategies to improve your marks and take control of your study.

- Workshops
- StudyWise
- Academic Integrity Module for Students
- Ask a Learning Adviser

# Student Services and Support

Students with a disability are encouraged to contact the **Disability Service** who can provide appropriate help with any issues that arise during their studies.

# **Student Enquiries**

For all student enquiries, visit Student Connect at ask.mq.edu.au

# IT Help

For help with University computer systems and technology, visit <u>http://informatics.mq.edu.au/hel</u>p/.

When using the University's IT, you must adhere to the <u>Acceptable Use Policy</u>. The policy applies to all who connect to the MQ network including students.

# **Graduate Capabilities**

# PG - Capable of Professional and Personal Judgment and Initiative

Our postgraduates will demonstrate a high standard of discernment and common sense in their professional and personal judgment. They will have the ability to make informed choices and decisions that reflect both the nature of their professional work and their personal perspectives.

This graduate capability is supported by:

#### Learning outcomes

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assessment tasks

- Assignment 1
- Assignment 2

- Assignment 3
- Assignment 4
- Assignment 5

# PG - Discipline Knowledge and Skills

Our postgraduates will be able to demonstrate a significantly enhanced depth and breadth of knowledge, scholarly understanding, and specific subject content knowledge in their chosen fields.

This graduate capability is supported by:

#### Learning outcomes

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assessment tasks

- Assignment 1
- Assignment 2
- Assignment 3
- Assignment 4
- Assignment 5

#### PG - Critical, Analytical and Integrative Thinking

Our postgraduates will be capable of utilising and reflecting on prior knowledge and experience, of applying higher level critical thinking skills, and of integrating and synthesising learning and knowledge from a range of sources and environments. A characteristic of this form of thinking is the generation of new, professionally oriented knowledge through personal or group-based critique of practice and theory.

This graduate capability is supported by:

#### Learning outcomes

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real

world" problem; identifying and applying appropriate mathematical techniques.

- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assessment tasks

- Assignment 1
- Assignment 2
- Assignment 3
- Assignment 4
- Assignment 5

#### PG - Research and Problem Solving Capability

Our postgraduates will be capable of systematic enquiry; able to use research skills to create new knowledge that can be applied to real world issues, or contribute to a field of study or practice to enhance society. They will be capable of creative questioning, problem finding and problem solving.

This graduate capability is supported by:

#### Learning outcomes

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assessment tasks

- Assignment 1
- Assignment 2
- Assignment 3
- Assignment 4
- Assignment 5

# PG - Effective Communication

Our postgraduates will be able to communicate effectively and convey their views to different social, cultural, and professional audiences. They will be able to use a variety of technologically supported media to communicate with empathy using a range of written, spoken or visual formats.

This graduate capability is supported by:

#### Learning outcomes

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- · 3. Expressing yourself clearly and logically in writing
- 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assessment tasks

- Assignment 1
- Assignment 2
- Assignment 3
- Assignment 4
- Assignment 5

# PG - Engaged and Responsible, Active and Ethical Citizens

Our postgraduates will be ethically aware and capable of confident transformative action in relation to their professional responsibilities and the wider community. They will have a sense of connectedness with others and country and have a sense of mutual obligation. They will be able to appreciate the impact of their professional roles for social justice and inclusion related to national and global issues

This graduate capability is supported by:

#### Learning outcomes

- 1. Understanding logical arguments and recognising any gaps or faults in such arguments.
- 2. Solving problems, including: formulating a precise mathematical question from a "real world" problem; identifying and applying appropriate mathematical techniques.
- 3. Expressing yourself clearly and logically in writing

 4. More broadly, you are expected to improve your generic skills in the following areas: literacy and numeracy, self-awareness and interpersonal skills, communications, critical analysis, problem solving and creative thinking.

#### Assessment tasks

- Assignment 1
- Assignment 2
- Assignment 3
- Assignment 4
- Assignment 5