



# STAT721

## Multivariate Analysis

S2 Evening 2017

*Dept of Statistics*

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## General Information

Unit convenor and teaching staff

Unit Convenor

Jun Ma

[jun.ma@mq.edu.au](mailto:jun.ma@mq.edu.au)

Contact via email

12 Wally's Walk (E7A), room 526

TBA

Credit points

4

Prerequisites

Admission to MRes

Corequisites

STAT710

Co-badged status

STAT721

Unit description

This unit studies basic methods of multivariate statistical analysis. Multivariate data arise when each unit of observation in the sample has more than one variable measured. Multivariate statistical analysis provides ways to analyse dependence structures within multivariate data, as well as to meaningfully simplify, classify and group such data. The unit introduces methodologies and techniques for the exploration and analysis of multivariate data. Topics include graphical displays, discriminant analysis, principal components analysis, multivariate normal distribution, multivariate linear models, cluster analysis.

## Important Academic Dates

Information about important academic dates including deadlines for withdrawing from units are available at <https://www.mq.edu.au/study/calendar-of-dates>

## Learning Outcomes

On successful completion of this unit, you will be able to:

Understand the fundamental difference between univariate and multivariate analysis.

Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.

Understand and be able to apply MANOVA.

Understand multivariate regression.

Know the theories of PCA and factor analysis, and be able to apply these methods to real data.

Understand likelihood based, as well as minimum expected cost based, discriminant analysis. Be able to apply these discriminant analysis methods to real data.

Understand the principles of classification tree and canonical analysis.

Know how to display multivariate data graphically using R.

Be able to use the R package for multivariate data analysis.

## General Assessment Information

### Assignment late submission

- Late submissions without approval will be penalized at a rate of 5% of earned mark per day, up to maximum of 50%. This implies that submissions will not be accepted more than 10 days late.
- Late submissions due to unavoidable disruptions must be approved and students are required to submit evidence for the disruptions.

## Assessment Tasks

Name	Weighting	Hurdle	Due
<a href="#"><u>Assignment 1</u></a>	15%	No	6pm on Sep 7, 2017
<a href="#"><u>Assignment 2</u></a>	15%	No	6pm on Nov 2, 2017
<a href="#"><u>Takehome examination</u></a>	45%	No	10am Nov 13, 2017
<a href="#"><u>Written Examination</u></a>	25%	No	University Exam period

### Assignment 1

Due: **6pm on Sep 7, 2017**

Weighting: **15%**

Assignment 1 will be available on the unit webpage in week 3 and due in the week 6 lecture. Assignments may be handwritten or word-processed, and submitted in person, or electronically via email to "jun.ma@mq.edu.au".

On successful completion you will be able to:

- Understand the fundamental difference between univariate and multivariate analysis.

- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
- Understand and be able to apply MANOVA.
- Know how to display multivariate data graphically using R.
- Be able to use the R package for multivariate data analysis.

## Assignment 2

Due: **6pm on Nov 2, 2017**

Weighting: **15%**

Assignment 2 will be available in week 9 and due in the week 12 lecture. Assignments may be handwritten or word-processed, and submitted in person, or electronically via email to "jun.ma@mq.edu.au".

On successful completion you will be able to:

- Understand multivariate regression.
- Know the theories of PCA and factor analysis, and be able to apply these methods to real data.
- Understand likelihood based, as well as minimum expected cost based, discriminant analysis. Be able to apply these discriminant analysis methods to real data.
- Understand the principles of classification tree and canonical analysis.
- Know how to display multivariate data graphically using R.
- Be able to use the R package for multivariate data analysis.

## Takehome examination

Due: **10am Nov 13, 2017**

Weighting: **45%**

For the **take-home** exam students will have THREE days to complete their exam papers. The exam paper will be available on unit web page at 10am on Friday 10th November, 2017 and the students must submit their answers before 10am, Monday November 13, 2017. This examination involves mainly analysis of real data sets and some simple theoretical questions and thus computer coding in R is required.

On successful completion you will be able to:

- Understand the fundamental difference between univariate and multivariate analysis.
- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
- Understand and be able to apply MANOVA.
- Understand multivariate regression.

- Know the theories of PCA and factor analysis, and be able to apply these methods to real data.
- Understand likelihood based, as well as minimum expected cost based, discriminant analysis. Be able to apply these discriminant analysis methods to real data.
- Understand the principles of classification tree and canonical analysis.
- Know how to display multivariate data graphically using R.
- Be able to use the R package for multivariate data analysis.

## Written Examination

Due: **University Exam period**

Weighting: **25%**

This is a written exam and it is to be scheduled in the university exam period. This examination mainly involves conceptual questions or simple calculation questions. For example, it may ask students to identify an appropriate hypothesis testing method for a particular data set. For this exam, students are allowed to bring into the exam room TWO A4 paper written/typed on both sides; photocopies **are not** allowed. Only non-programmable calculators that do not have text retrieval capacity are allowed. Students who apply Supplementary Exams must make themselves available during supplementary exam period from 11/12/17 to 15/12/17.

On successful completion you will be able to:

- Understand the fundamental difference between univariate and multivariate analysis.
- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
- Understand and be able to apply MANOVA.
- Understand multivariate regression.
- Know the theories of PCA and factor analysis, and be able to apply these methods to real data.
- Understand likelihood based, as well as minimum expected cost based, discriminant analysis. Be able to apply these discriminant analysis methods to real data.
- Be able to use the R package for multivariate data analysis.

## Delivery and Resources

### Classes

You are required to attend a 3-hour lecture each week; the time and room are:

Thursday                  6pm – 9pm                  [6 Eastern Rd \(E4B\) Faculty PC Lab](#)

## Technologies used and required

We primarily use the software package R in this Unit. R is becoming increasingly important for statisticians and other scientists. More information about R can be found at the web site <http://www.r-project.org/> and the package can be downloaded **free of charge** from there. R is very similar to the package S-PLUS and most of its codes will also work in S-Plus. From week 2, students will be given exercises each week covering materials from the lectures, and most exercises require using R.

## Recommended texts

**Prescribed textbook:** “**Applied Multivariate Statistical Analysis**” by Richard A. Johnson, Dean W. Wichern (6<sup>th</sup> edition)

Students are expected to possess a copy of this textbook and are required to read certain book chapters each week. The following books may be used as other references for this unit:

DILLON & GOLDSTEIN      Multivariate Analysis – Methods and applications(QA 278 .d55)

FAHRMEIR & TUTZ              Multivariate statistical modelling based on generalized linear models (QA 278 .F34)

FLURY, B                              A first course in multivariate statistics

FLURY, B                              Multivariate statistics: A practical approach

MORRISON, D                      Multivariate statistical methods

## Unit Schedule

The following is a detailed list of the topics covered in this Unit, together with the planned delivery time. All lecture notes will be available on iLearn prior to the lecture.

Week	Topic
1	<ol style="list-style-type: none"> <li>1. Introduction to multivariate analysis</li> <li>2. Overview of matrix algebra</li> </ol>
2	<ol style="list-style-type: none"> <li>1. Matrix algebra (cont.)</li> <li>2. Basic concepts of multivariate distributions</li> <li>3. Sample statistics</li> </ol>
3	<ol style="list-style-type: none"> <li>1. Multivariate sample statistics (cont.)</li> <li>2. Some useful multivariate distributions</li> </ol>

4.	<ol style="list-style-type: none"> <li>1. Initial data analysis</li> <li>2. Inferences: Estimation and hypothesis testing</li> </ol>
5.	<ol style="list-style-type: none"> <li>1. Inferences (cont.)</li> </ol>
6.	<ol style="list-style-type: none"> <li>2. MANOVA</li> </ol>
7.	<ol style="list-style-type: none"> <li>1. MANOVA (cont.)</li> <li>2. Multivariate regression</li> </ol>
8.	<ol style="list-style-type: none"> <li>1. Regression (cont.)</li> <li>2. Principal component analysis (PCA)</li> </ol>
9.	<ol style="list-style-type: none"> <li>1. Factor analysis (FA)</li> </ol>
11.	<ol style="list-style-type: none"> <li>1. Factor analysis (cont.)</li> <li>2. Discriminant analysis and classification</li> </ol>
12.	<ol style="list-style-type: none"> <li>1. Discriminant analysis (cont.)</li> </ol>
13.	<ol style="list-style-type: none"> <li>1. Brief introduction to canonical correlation analysis</li> <li>2. Brief introduction to cluster analysis</li> </ol>

## Policies and Procedures

Macquarie University policies and procedures are accessible from [Policy Central](#). Students should be aware of the following policies in particular with regard to Learning and Teaching:

Academic Honesty Policy [http://mq.edu.au/policy/docs/academic\\_honesty/policy.html](http://mq.edu.au/policy/docs/academic_honesty/policy.html)

Assessment Policy [http://mq.edu.au/policy/docs/assessment/policy\\_2016.html](http://mq.edu.au/policy/docs/assessment/policy_2016.html)

Grade Appeal Policy <http://mq.edu.au/policy/docs/gradeappeal/policy.html>

Complaint Management Procedure for Students and Members of the Public [http://www.mq.edu.au/policy/docs/complaint\\_management/procedure.html](http://www.mq.edu.au/policy/docs/complaint_management/procedure.html)

Disruption to Studies Policy (in effect until Dec 4th, 2017): [http://www.mq.edu.au/policy/docs/disruption\\_studies/policy.html](http://www.mq.edu.au/policy/docs/disruption_studies/policy.html)

Special Consideration Policy (in effect from Dec 4th, 2017): <https://staff.mq.edu.au/work/strategy-planning-and-governance/university-policies-and-procedures/policies/special-consideration>

In addition, a number of other policies can be found in the [Learning and Teaching Category](#) of Policy Central.

## Student Code of Conduct

Macquarie University students have a responsibility to be familiar with the Student Code of Conduct: [https://students.mq.edu.au/support/student\\_conduct/](https://students.mq.edu.au/support/student_conduct/)

## Results

Results shown in *iLearn*, or released directly by your Unit Convenor, are not confirmed as they are subject to final approval by the University. Once approved, final results will be sent to your student email address and will be made available in [eStudent](#). For more information visit [ask.mq.edu.au](http://ask.mq.edu.au).

## Student Support

Macquarie University provides a range of support services for students. For details, visit <http://students.mq.edu.au/support/>

## Learning Skills

Learning Skills ([mq.edu.au/learningskills](http://mq.edu.au/learningskills)) provides academic writing resources and study strategies to improve your marks and take control of your study.

- [Workshops](#)
- [StudyWise](#)
- [Academic Integrity Module for Students](#)
- [Ask a Learning Adviser](#)

## Student Services and Support

Students with a disability are encouraged to contact the [Disability Service](#) who can provide appropriate help with any issues that arise during their studies.

## Student Enquiries

For all student enquiries, visit Student Connect at [ask.mq.edu.au](http://ask.mq.edu.au)

## IT Help

For help with University computer systems and technology, visit [http://www.mq.edu.au/about\\_us/offices\\_and\\_units/information\\_technology/help/](http://www.mq.edu.au/about_us/offices_and_units/information_technology/help/).

When using the University's IT, you must adhere to the [Acceptable Use of IT Resources Policy](#). The policy applies to all who connect to the MQ network including students.

## Graduate Capabilities

### PG - Discipline Knowledge and Skills

Our postgraduates will be able to demonstrate a significantly enhanced depth and breadth of knowledge, scholarly understanding, and specific subject content knowledge in their chosen fields.



This graduate capability is supported by:

## Learning outcomes

- Understand the fundamental difference between univariate and multivariate analysis.
- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
- Understand and be able to apply MANOVA.
- Understand multivariate regression.
- Know the theories of PCA and factor analysis, and be able to apply these methods to real data.
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- Understand the principles of classification tree and canonical analysis.
- Know how to display multivariate data graphically using R.
- Be able to use the R package for multivariate data analysis.

## Assessment tasks

- Assignment 1
- Assignment 2
- Takehome examination
- Written Examination

## PG - Critical, Analytical and Integrative Thinking

Our postgraduates will be capable of utilising and reflecting on prior knowledge and experience, of applying higher level critical thinking skills, and of integrating and synthesising learning and knowledge from a range of sources and environments. A characteristic of this form of thinking is the generation of new, professionally oriented knowledge through personal or group-based critique of practice and theory.

This graduate capability is supported by:

## Learning outcomes

- Understand the fundamental difference between univariate and multivariate analysis.
- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
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- Understand multivariate regression.
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- Understand the principles of classification tree and canonical analysis.
- Know how to display multivariate data graphically using R.

## **Assessment tasks**

- Assignment 1
- Assignment 2
- Takehome examination
- Written Examination

## **PG - Research and Problem Solving Capability**

Our postgraduates will be capable of systematic enquiry; able to use research skills to create new knowledge that can be applied to real world issues, or contribute to a field of study or practice to enhance society. They will be capable of creative questioning, problem finding and problem solving.

This graduate capability is supported by:

## **Learning outcomes**

- Understand the fundamental difference between univariate and multivariate analysis.
- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
- Understand and be able to apply MANOVA.
- Understand multivariate regression.
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- Know how to display multivariate data graphically using R.
- Be able to use the R package for multivariate data analysis.

## **Assessment tasks**

- Assignment 1
- Assignment 2
- Takehome examination

## PG - Effective Communication

Our postgraduates will be able to communicate effectively and convey their views to different social, cultural, and professional audiences. They will be able to use a variety of technologically supported media to communicate with empathy using a range of written, spoken or visual formats.

This graduate capability is supported by:

### Learning outcomes

- Know how to perform hypothesis testing (mainly the Hotelling T2 test) involving multivariate data.
- Understand and be able to apply MANOVA.
- Understand multivariate regression.
- Know the theories of PCA and factor analysis, and be able to apply these methods to real data.
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### Assessment tasks

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