

# STAT7310 Statistical Theory

Session 1, In person-scheduled-weekday, North Ryde 2024

School of Mathematical and Physical Sciences

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#### Disclaimer

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#### **General Information**

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Second Unit Convenor/Lecturer Connor Smith connor.smith@mq.edu.au Contact via Email please refer to iLearn

Credit points 10

Prerequisites Admission to MRes

Corequisites

Co-badged status STAT8310

Unit description

This unit introduces the foundation concepts of probability and statistics. The unit develops probability concepts, including random variables and distributions, independence, joint and conditional distributions, expectations, generating functions, distributions of sums of independent random variables and the Central Limit Theorem. The principles of statistical inference are discussed with a particular focus on point estimators, confidence intervals and hypothesis testing.

#### Important Academic Dates

Information about important academic dates including deadlines for withdrawing from units are available at <a href="https://www.mq.edu.au/study/calendar-of-dates">https://www.mq.edu.au/study/calendar-of-dates</a>

## Learning Outcomes

On successful completion of this unit, you will be able to:

ULO1: Apply concepts related to probability and statistics including random variables

and distributions, independence, joint and conditional distributions, expectations, generating functions, distributions of sums of independent random variables and the Central Limit Theorem.

**ULO2:** Summarise data using appropriate statistical analysis, descriptive statistics and graphical presentation.

**ULO3:** Evaluate the appropriateness of a variety of statistical models/methods for various types of data, apply them, and interpret the results.

**ULO4:** Apply concepts related to statistical inference including point estimators, confidence intervals and hypothesis testing.

### **General Assessment Information**

To pass this unit you must achieve a total mark equal to or greater than 50%.

There are no hurdle assessments for this unit.

The online quiz, test and exam must be undertaken at the time indicated in the unit guide or on iLearn. Should these activities be missed due to illness or misadventure, students may apply for special consideration.

**ASSIGNMENT SUBMISSION**: Assignment submission will be online through the iLearn page.

Submit assignments online via the appropriate assignment link on the iLearn page. A personalised cover sheet is not required with online submissions. Read the submission statement carefully before accepting it as there are substantial penalties for making a false declaration.

- Assignment submission is via iLearn. You should upload this as a single scanned PDF file.
- Please note the quick guide on how to upload your assignments provided on the iLearn page.
- Please make sure that each page in your uploaded assignment corresponds to only one A4 page (do not upload an A3 page worth of content as an A4 page in landscape). If you are using an app like Clear Scanner, please make sure that the photos you are using are clear and shadow-free.
- It is your responsibility to make sure your assignment submission is legible.
- If there are technical obstructions to your submitting online, please email us to let us know.

You may submit as often as required prior to the due date/time. The assisgnment must be submitted by 11:55 pm on its due date. Please note that each submission will completely replace any previous submissions. It is in your interests to make frequent submissions of your partially completed work as insurance against technical or other problems near the submission deadline.

**LATE SUBMISSION OF WORK:** Unless a Special Consideration request has been submitted and approved, a 5% penalty (of the total possible mark) will be applied each day a written assessment is not submitted, up until the 7th day (including weekends). After the 7th day, a grade of '0' will be awarded even if the assessment is submitted. Submission time for all written assessments is set at 11:55 pm. A 1-hour grace period is provided to students who experience a technical concern.

For any late submission of time-sensitive tasks, such as scheduled tests and exams, students need to submit an application for <u>Special Consideration</u>.

In this unit, late submissions will be accepted as follows:

- · iLearn Quiz NO, unless Special Consideration is granted
- · Test NO, unless Special Consideration is granted
- Assignment YES, Standard Late Penalty applies
- · Final Examination NO, unless Special Consideration is granted

**SPECIAL CONSIDERATION:** The <u>Special Consideration Policy</u> aims to support students who have been impacted by short-term circumstances or events that are serious, unavoidable and significantly disruptive, and which may affect their performance in assessment. If you experience circumstances or events that affect your ability to complete the assessments in this unit on time, please inform the convenor and submit a Special Consideration request through ask.mq.edu.au.

**FINAL EXAM POLICY:** It is Macquarie University policy not to set early examinations for individuals or groups of students. All students are expected to ensure that they are available until the end of the teaching semester, that is, the final day of the official examination period. The only excuse for not sitting an examination at the designated time is because of documented illness or unavoidable disruption. In these special circumstances, you may apply for special consideration via ask.mq.edu.au.

If you receive special consideration for the final exam, a supplementary exam will be scheduled in the interval between the regular exam period and the start of the next session. By making a special consideration application for the final exam you are declaring yourself available for a resit during this supplementary examination period and will not be eligible for a second special consideration approval based on pre-existing commitments. Please ensure you are familiar with the policy prior to submitting an application.

Name	Weighting	Hurdle	Due
iLearn Quiz	5%	No	Week 5
Test	20%	No	Week 7
Assignment	15%	No	Week 11

#### **Assessment Tasks**

Name	Weighting	Hurdle	Due
Final Examination	60%	No	University Examination Period

#### iLearn Quiz

Assessment Type 1: Quiz/Test Indicative Time on Task 2: 1 hours Due: **Week 5** Weighting: **5%** 

#### iLearn Quiz

On successful completion you will be able to:

 Apply concepts related to probability and statistics including random variables and distributions, independence, joint and conditional distributions, expectations, generating functions, distributions of sums of independent random variables and the Central Limit Theorem.

#### Test

Assessment Type 1: Quiz/Test Indicative Time on Task 2: 1 hours Due: **Week 7** Weighting: **20%** 

Mid-Semester Class Test

On successful completion you will be able to:

 Apply concepts related to probability and statistics including random variables and distributions, independence, joint and conditional distributions, expectations, generating functions, distributions of sums of independent random variables and the Central Limit Theorem.

#### Assignment

Assessment Type 1: Quantitative analysis task Indicative Time on Task 2: 8 hours Due: **Week 11**  Unit guide STAT7310 Statistical Theory

Weighting: 15%

#### Assignment

On successful completion you will be able to:

- Summarise data using appropriate statistical analysis, descriptive statistics and graphical presentation.
- Evaluate the appropriateness of a variety of statistical models/methods for various types of data, apply them, and interpret the results.
- Apply concepts related to statistical inference including point estimators, confidence intervals and hypothesis testing.

#### **Final Examination**

Assessment Type 1: Examination Indicative Time on Task 2: 3 hours Due: **University Examination Period** Weighting: **60%** 

Invigilated Final Examination

On successful completion you will be able to:

- Apply concepts related to probability and statistics including random variables and distributions, independence, joint and conditional distributions, expectations, generating functions, distributions of sums of independent random variables and the Central Limit Theorem.
- Summarise data using appropriate statistical analysis, descriptive statistics and graphical presentation.
- Evaluate the appropriateness of a variety of statistical models/methods for various types of data, apply them, and interpret the results.
- Apply concepts related to statistical inference including point estimators, confidence intervals and hypothesis testing.

<sup>1</sup> If you need help with your assignment, please contact:

- the academic teaching staff in your unit for guidance in understanding or completing this type of assessment
- the Writing Centre for academic skills support.

<sup>2</sup> Indicative time-on-task is an estimate of the time required for completion of the assessment task and is subject to individual variation

## **Delivery and Resources**

#### Technologies used and required

The unit is delivered by lectures (2 hours per week, starting in Week 1) and SGTAs (1 hour per week, starting in Week 2). All teaching material will be available on iLearn.

SGTA exercises will be available from iLearn prior to the SGTA. Students are expected to have attempted these prior to the SGTA. Solutions will be explained, with emphasis on any area students had trouble with. At the end of the week, these solutions will then be placed on iLearn. The web address is https://ilearn.mq.edu.au.

The R software (freely available online) will be used in the unit. Students need to practice how to use the software and be expected to use R for the assignment. Students should also note that the test and the final examination may contain inline R codes and output that students need to interpret to answer the questions.

#### Required and Recommended texts and/or materials

There is no required textbook for this unit. Students may benefit from having access to the following background reference for additional reading and problems:

 "Mathematical Statistics with Applications" W Mendenhall, D Wackerly and R Scheaffer (6th or 7th edition) - library call number is QA276.M426.

The following books may also be useful background references:

- CASELLA, G. & BERGER, R.L. Statistical Inference (QA276.C37)
- FREUND, J. E. Mathematical Statistics (QA276.F692)
- HOEL, P. Introduction to Mathematical Statistics (QA276.H57)
- HOGG, R.V. & CRAIG, A.T. Introduction to Mathematical Statistics (QA276.H59)
- HOGG, R.V. & TANIS, E.A. Probability and Statistical Inference (QA273.H694)
- LARSON, H. Introduction to Probability Theory and Statistical Inference (QA273.L352)
- ROSS, S. A First Course in Probability (QA273.R83)
- SCHEAFFER, R. L. Introduction to Probability and Its Applications (QA273.S357)
- SMITH, P. J. Into Statistics (QA276.S615)
- SPIEGEL, M.R., SRINIVASAN, J. & SCHILLER, J.J. Schaum's outline of theory and problems of probability and statistics (QA273.25.S64)

 WALPOLE, R.E. & MYERS, R.H. Probability and Statistics for Engineers and Scientists (TA340.W35)

At least one copy of each of these is available in the Library, and extra copies may be available on the shelves for borrowing purposes.

It should be understood that there are variations in notation (and even in definition) from one reference book to another, and that the lecture material alone defines recommended notation. Note that all lecture notes will be available in pdf form on the Unit website on iLearn before the lecture. You are required to bring a hard or soft copy of the lecture notes to lectures.

### Methods of Communication

We will communicate with you via your university email or through announcements on iLearn. Queries to the convenor can either be placed on the iLearn discussion board or sent to the staff email address from your university email address.

### **COVID** Information

For the latest information on the University's response to COVID-19, please refer to the Coronavirus infection page on the Macquarie website: <a href="https://www.mq.edu.au/about/coronavirus-faqs">https://www.mq.edu.au/about/coronavirus-faqs</a>. Remember to check this page regularly in case the information and requirements change during semester. If there are any changes to this unit in relation to COVID, these will be communicated via iLearn.

## **Unit Schedule**

TOPIC	MATERIAL COVERED
1	Sample space, events. Axioms of probability, conditional probability. Bayes Theorem.
2	Random variables and probability distributions. Standard discrete and continuous distributions and their key characteristics. The Poisson process.
3	Expected values (discrete and continuous) and their properties. Measures of variation. Quantiles. Moments (raw and central). Interpretation of moments (skewness, kurtosis etc.).
4	Sums of independent random variables. Discrete and continuous convolutions with applications. Transformations (monotonic and non-monotonic) of continuous random variables. Transformation of a continuous random variable to one with a uniform distribution, with applications to simulation.
5	Probability generating functions and moment generating functions with properties and applications. The moment generating function of a sum of independent random variables. The Central Limit Theorem and applications.
6	Multivariate (particularly bivariate) random variable theory (continuous and discrete). Marginal and conditional distributions and expectations. Covariance and correlation.
7	Exploratory data analysis including measures of association and principal component analysis.

8	Random sampling and sampling distributions.
9	Point estimators and their properties. MLEs and asymptotic results and bootstrapping.
10	Interval estimators, their properties.
11	Hypothesis testing, including likelihood ratios and goodness of fit.

## **Policies and Procedures**

Macquarie University policies and procedures are accessible from Policy Central (https://policie s.mq.edu.au). Students should be aware of the following policies in particular with regard to Learning and Teaching:

- Academic Appeals Policy
- Academic Integrity Policy
- Academic Progression Policy
- Assessment Policy
- Fitness to Practice Procedure
- Assessment Procedure
- Complaints Resolution Procedure for Students and Members of the Public
- Special Consideration Policy

Students seeking more policy resources can visit <u>Student Policies</u> (<u>https://students.mq.edu.au/su</u> <u>pport/study/policies</u>). It is your one-stop-shop for the key policies you need to know about throughout your undergraduate student journey.

To find other policies relating to Teaching and Learning, visit <u>Policy Central</u> (<u>https://policies.mq.e</u> <u>du.au</u>) and use the <u>search tool</u>.

#### **Student Code of Conduct**

Macquarie University students have a responsibility to be familiar with the Student Code of Conduct: https://students.mq.edu.au/admin/other-resources/student-conduct

#### **Results**

Results published on platform other than <u>eStudent</u>, (eg. iLearn, Coursera etc.) or released directly by your Unit Convenor, are not confirmed as they are subject to final approval by the University. Once approved, final results will be sent to your student email address and will be made available in <u>eStudent</u>. For more information visit <u>ask.mq.edu.au</u> or if you are a Global MBA student contact globalmba.support@mq.edu.au

#### Academic Integrity

At Macquarie, we believe <u>academic integrity</u> – honesty, respect, trust, responsibility, fairness and courage – is at the core of learning, teaching and research. We recognise that meeting the

expectations required to complete your assessments can be challenging. So, we offer you a range of resources and services to help you reach your potential, including free <u>online writing an</u> d maths support, academic skills development and wellbeing consultations.

### Student Support

Macquarie University provides a range of support services for students. For details, visit <u>http://stu</u> dents.mq.edu.au/support/

#### **The Writing Centre**

The Writing Centre provides resources to develop your English language proficiency, academic writing, and communication skills.

- Workshops
- Chat with a WriteWISE peer writing leader
- Access StudyWISE
- Upload an assignment to Studiosity
- Complete the Academic Integrity Module

The Library provides online and face to face support to help you find and use relevant information resources.

- Subject and Research Guides
- Ask a Librarian

#### Student Services and Support

Macquarie University offers a range of Student Support Services including:

- IT Support
- · Accessibility and disability support with study
- Mental health support
- Safety support to respond to bullying, harassment, sexual harassment and sexual assault
- · Social support including information about finances, tenancy and legal issues
- <u>Student Advocacy</u> provides independent advice on MQ policies, procedures, and processes

#### **Student Enquiries**

Got a question? Ask us via AskMQ, or contact Service Connect.

#### IT Help

For help with University computer systems and technology, visit <u>http://www.mq.edu.au/about\_us/</u>offices\_and\_units/information\_technology/help/.

When using the University's IT, you must adhere to the <u>Acceptable Use of IT Resources Policy</u>. The policy applies to all who connect to the MQ network including students.

Unit information based on version 2024.01R of the Handbook